A Hybrid Approach for Single Objective Job Shop Scheduling Problems

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Abstract: Scheduling problems are usually solved using optimization techniques to get optimal or near optimal solutions because problems found in practical applications cannot be solved to optimality using reasonable resources in many cases. The n-job, m-machine Job shop scheduling (JSP) problem is one of the general production scheduling problems. In this paper, optimization of practical performance measure of makespan is considered. Hybrid approach is proposed to solve JSP problems. The hybrid approach is tested with 10 benchmark JSP problems in finding optimal makespan values. The results of hybrid approach are compared with Artificial Immune System (AIS), Tabu Search Shifting Bottleneck approach (TSSB) approach. The performance of hybrid approach is efficient in finding optimal solutions compared to that of other approaches reported in literature.


Key words: Job Shop Scheduling, Hybrid Approach, Benchmark Problems

1. INTRODUCTION

The job shop problem is the most complicated and typical problem of all kinds of production scheduling problems, the allocation of resources over time to perform a collection of tasks (Alqahtani and Saba, 2013). Job shop scheduling can be stated as follows: given n jobs that have to be processed on m machines in a prescribed order under certain restrictive assumptions. The objective is to decide how to arrange the processing orders and starting times of operations sharing the same machine. Manufacturing systems with objectives require optimization criteria, such as stock size, due-date reliability and mean lead time.

The classical job-shop scheduling problem is one of the most difficult combinatorial optimization problems (Brucker, 1995). Issues concerning the content and scope of JSPs have been attracting much attention from researchers and practitioners. Mathematical and heuristic methods are the two major methods for resolving JSP. Optimization methods attempt to find the optimal solution through mathematical programming techniques or methods (Rehman and Saba, 2012b,c; Brucker et al, 1994). However, mathematical programming methods are time-consuming, and thus many researchers focus on developing heuristic algorithms. Heuristic algorithms in common use include shifting bottleneck (SB) (Rehman and Saba,2012a), Tabu search (TS) (Saba and Almatneem, 2013; Saba and Alqahtani,2013), Simulated annealing (SA) (Saba et al., 2012; Krishan et al, 1995; Steinhofel et al, 1999), Genetic algorithm (GA) (Zhou et al, 2001) and Artificial Immune System (AIS) (Rehman and Saba,2012c). During the last decades a great deal of attention has been paid to solving these problems with many kinds of algorithms by considering single objective (Saba and Rehman, 2012a).

Additionally, research on job shop scheduling problems was concentrated primarily on the optimization of individual measures of system performance. While a single objective may be justified in certain situations Lee and Jung (1989), Murata, Ishibuchi, and Tanaka (1996) and Chandrasekaran et al (2006).

2. JOB SHOP SCHEDULING PROBLEM

Normally, the entire job-shop scheduling problem consists of two types of constraints: sequence constraint and resource constraint (Sulong et al., 2010; Saba and Rehman, 2012). The first type states that two operations of a job cannot be processed at the same time. The second type states that no more than one job can be handled on a machine at the same time. Job-shop scheduling can be viewed as an optimization problem, bounded by both sequence and resource constraints. For a job-shop scheduling problem, each job may consist of different number of operations, subjected to some precedence restrictions (Rehman and Saba,2011). Commonly the processing orders of each job by all machines and the processing time of each operation are known and fixed. Once started operations cannot be interrupted. Assume job i(i=1,2,…,n) requires processing by machine k(k=1,2,…,m) exactly once in its operation sequence (thus, each job has m operations).Let pik is the processing time of job i on...
machine k, Xik is the starting time of job i on machine k, qik is the indicator which takes on a value of 1 if operation j of job i requires machine k, and zero otherwise. Yihk is the variable which takes on a value of 1 if job precedes job h on machine k, and zero otherwise. The objective function for the given Job Shop Scheduling is

\[
\text{Minimize } Z = C_{\text{max}}
\]

Subject to

a) **Sequence constraint**

ie., for a given job i, the (j+1)st operation may not start before the jth operation is completed.

b) **Resource constraint**

ie. Only one job will be processed in a machine.

### 3. PROPOSED HYBRID ALGORITHM FOR JOB SHOP SCHEDULING PROBLEM

In the proposed hybrid algorithm initial sequence is processed with AIS algorithm and finally results are refined with SFHM algorithm. The operative mechanisms of immune system are very efficient from a computational standpoint. The artificial immune system was built on the following two principles of the immune system. a) Clonal selection principle b) Affinity maturation principle

In sheep flocks heredity model algorithm special string structure, hierarchical genetic operations (crossover and mutation) are introduced. They are (1) sub-chromosome level genetic operation and (2) chromosome (global) level genetic operation. This hierarchical operation is referred to as "multi-stage genetic operation".

Generate a population of P antibodies (job sequences)

**Stage 1 (AIS Algorithm)**

For each iteration

Select the sequence in the antibody population;

Find out the affinity of each antibody;

Cloning process (generate copies of the antibodies)

**Steps in Mutation process** (for each clone)

Find inverse mutation

Select the new sequence obtained from inverse mutation

Find the makespan of the new sequence

if (makespan (new sequence) = = makespan (clone))
then if ( tardiness(new sequence) < tardiness (clone))
clone = new sequence;
else clone = clone;
if makespan (new sequence) < makespan (clone) then
Clone = new sequence
else do pair wise interchange
select the new sequence
Find the makespan of the new sequence
if (makespan (new sequence) = = makespan (clone))
then if ( tardiness(new sequence) < tardiness (clone))
clone = new sequence
else clone = clone
If makespan (new sequence) < makespan (clone) then
clone = new sequence:
else clone = clone
antibody = clone

Eliminate worst %B number of antibodies in the population
Create new antibodies at the same number (%B of pop.)
change the eliminated ones with the new created ones while stopping criteria = false.

**Stage 2: (SFHM Algorithm)**

Use the population from AIS algorithm,

Select the parent
Sub chromosome level crossover
Set sub chromosome level crossover probability
If population probability is less than or equal to sub chromosome level probability
Perform sub chromosome level crossover
Else retain the old sequences
Sub chromosome level mutation
Set sub chromosome mutation probability
If population probability is less than or equal to sub chromosome mutation probability
Perform sub chromosome level mutation
Else retain the same sequences
Select two sequences from population
Chromosome level crossover
Set crossover probability
If population probability is less than or equal to crossover probability
Perform chromosome level crossover
Else retain the same sequences
Chromosome level mutation
Set mutation probability
If population probability is less than or equal to mutation probability
Perform chromosome level mutation
Else retain the same sequences
End if terminal condition satisfied
4. RESULTS AND DISCUSSION

The proposed hybrid algorithm has been tested for 10 problem instances of various sizes collected in the following classes:

**TABLE 1. Results of ten job shop scheduling problems**

<table>
<thead>
<tr>
<th>Problem</th>
<th>n</th>
<th>m</th>
<th>Hybrid</th>
<th>AIS</th>
<th>TSSB</th>
</tr>
</thead>
<tbody>
<tr>
<td>ORB1</td>
<td>10</td>
<td>10</td>
<td>1059</td>
<td>1062</td>
<td>1064</td>
</tr>
<tr>
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<td>10</td>
<td>10</td>
<td>888</td>
<td>891</td>
<td>890</td>
</tr>
<tr>
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<td>10</td>
<td>1005</td>
<td>1005</td>
<td>1013</td>
</tr>
<tr>
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<td>2759</td>
<td>2760</td>
<td>2760</td>
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</tbody>
</table>
In Table 1, the solutions for job shop problems obtained from hybrid are compared with AIS, TSSB procedure. Hybrid gives optimum value than AIS and TSSB procedure.

5. CONCLUSION
In this paper, the proposed hybrid approach has been used for solving job shop scheduling problem with the objective of makespan minimization. The hybrid approach uses simple but effective techniques for calculating cloning process, applying mutations a receptor editing procedure and SFHM Algorithm. The algorithm has been tested on 10 benchmark problem instances. The findings were compared with Artificial Immune System, Tabu Search Shifting Bottleneck procedure. The proposed hybrid approach found better results in most of the problems.

References

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